

**PRINCIPAL COMPONENT ANALYSIS OF CRIME DATA IN GWAGWALADA  
AREA COMMAND, ABUJA FROM 1995 – 2014****Nasiru M.O, S.O. Adams and A.I. Alumbugu**Department of Statistics, University of Abuja, Abuja  
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**ABSTRACT:** *This paper analyses Abuja crime data which consists of the averages of twenty major crimes reported to the police for the period 1995 – 2014. Correlation analysis and principal component analysis (PCA) were employed to explain the correlation between the crimes and to determine the distribution of the crimes over the three Area Councils under the Gwagwalada Area Command. The result has shown a significant correlation between robbery and rape, grievous hurt and wound (GHW), theft, assault, murder and unlawful escape. Gwagwalada Area Council has the overall crime rate in the Area Command. Rape is more prevalence in Kwali Area Council while unlawful possession and escape is more prevalence in Kuje Area Council Area. The PCA has suggested retaining four components that explain about 94.32 percent of the total variability of the data set.*

**KEYWORDS:** Multivariate Analysis, Factor Analysis; PCA, GHW, DPHs

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**INTRODUCTION**

In recent time there has been an increase in the reported cases of crime across the country consequently in the FCT Abuja, thus raising the issue of what categories of crime is committed in the federal capital territory. The scope of crime prevention has grown considerably in the last few years. What was previously the sole concern of the police and the private security industry has spread into areas from real estate developer, car manufacturers, residents' groups, building public facilities like society offices and shopping centers, all these calls for continuously using improved new ways to prevent crime. Criminal victimization has serious consequences for the citizens and society because high standard of living is undermined by high level of criminal victimization (Alemika and Chukwuma, 2005). The issue of crime in the city of Abuja has increase since the relocation of the federal capital to Abuja, the statistical analysis of the crime rate in Abuja will be explain and analyzed as Crime is one of the continuous problems that bedevil the existence of mankind. Principal component analysis (PCA) is very useful in crime analysis because of its robustness in data reduction and in determining the overall criminality in a given geographical area. PCA is a data analysis tool that is usually used to reduce the dimensionality (number of variable) of a large number of interrelated variables while retaining as much of the information (variation) as possible.

Literature has shown that previous research on crime data were analyzed using Principal Component Analysis (PCA). (Kendall Williams et al, 2004), classified a city as safe or unsafe in the US Cities by using multivariate methods of principal components, factor analysis, and discriminant analysis to reduce the 14 distinct variables that can affect the crime rate of a city to 6 and 7 important variables that show a high correlation with all the variables. Principal component analysis did decrease the number of variables to 6 and accounted for 86% of the total variance, while factor analysis decreased the number to 7 and accounted for 79.7% of the total variance.

(Olufolabo et. al, 2015), analyzed Oyo State crime data which consists of 8 major crime reported to the police between the period of 1996-2014. They employed correlation analysis and principal component analysis to explain the correlation between the crimes in the state. Their results showed a significant correlation, the principal component analysis has suggested retaining 6 components that explained about 83.79% of the total variability of the data set.

(Yusuf Bello et al, 2014), in their research employed the method of face-to-face personal interview using a stratified multistage random selection procedure. They applied PCA to analyze the spatial pattern of criminal victimization in the 11 Local Government Areas in Kastina Senatorial Zone. They found out that Batsari has the overall highest average victimization while Rimi has the lowest average victimization in the zone.

(Shehu et al, 2012), used katsina state data which consist of the average of eight major crimes reported to the police for the period 2006 – 2008. Correlation analysis and principal component analysis (PCA) were employed to explain the correlation between the crimes and to determine the distribution of the crimes over the local government of the state. The result has shown a significant correlation between robbery, theft and vehicle theft. The PCA has suggested retaining four components that explain about 78.94 percent of the total variability of the data set.

This paper explores the use of correlation analysis and PCA for effective crime control and prevention. PCA offers a tool for reducing the dimensionality of a very large data set and in determining the areas with overall crime rate. These if properly implemented, will successively solve many of the complex criminal problems that have bedeviled the country in general and Abuja in particular.

The objectives of this research include:

- (i) to determine the bivariate association existing between pairs of crime types.
- (ii) to identify the crime that's dominant in Gwagwalada Area Command, FCT Abuja
- (ii) to reduce the dimension of the data using Principal Component Analysis (PCA).
- (iii) to classify the crime type

### **Data Description**

The total number of crime committed yearly within the period 1995 – 2014 for the 3 Divisional Police Headquarters (DPHs) or the 3 selected Area Councils in Abuja was collected officially from the FCT Police Headquarters, Abuja. For easy statistical analysis and interpretation, the 3 Area Councils (AC) were categorized according. The three (3) area councils under the Gwagwalada Area Command are Gwagwalada, Kuje and Kwali. The data consists of thirteen major crimes reported to the police within the period 1995 – 2014. The crime include; rape, robbery, Grievous Hurt and Wound (GHW), theft, Vehicle theft, assault, murder, car stealing, unlawful possession, breach of peace, broken store and unlawful escape.

Frequencies of crimes for each category were averaged over the ten years in the study period to control for anomalous years when there may have been an unexplained spike or fall in crime levels prior to the statistical analysis. The value for each crime was converted to crime rate per 100,000 populations of the Area Council (AC) which was calculated as (Kpedekpo and Arya, 1981).

$$\text{Crime Rate} = \frac{\text{Number of Crime committed}}{\text{Population of the ACs}} \times 100,000$$

## METHODOLOGY

### Principal Component Analysis

Principal component analysis (PCA) is one of the most frequently used multivariate data analysis and it can be consider as a projection method which project observations from a p-dimensional space with p-variable to a k-dimensional space (where  $K < P$ ) so as to conserve the maximum amount of information (information is measured here through the total variance of the scatter plots) from the initial dimensions. This method transforms a set of highly correlated variable into the new sets which are uncorrelated but contain almost all information in the original data. The new set of variables are often fewer in number than original variables. The features of PCA are; it incorporate no error terms in its structure and hence it is a mathematical procedure, It transforms a set of variable into a new set of uncorrelated variables, It is appropriate when variables are on equal footing.

### Derivation of PCA

Given a P dimensional random vector  $X_i = (X_1, X_2, \dots, X_p)$  with mean vector  $\mu_i = (\mu_1, \mu_2, \dots, \mu_p)$  and dispersion matrix  $\Sigma$ , PCA seeks a new set variable  $Z_1, Z_2, \dots, Z_p$  (P' often fewer than P) so that:

$$Z_j = a_{1j}X_1 + a_{2j}X_2 + \dots + a_{pj}X_p = a_{ij}X \quad (3.1)$$

Where;  $j=1,2,\dots,p$  and  $a_{ij} = (a_{1j}, a_{2j}, \dots, a_{pj})$  are coefficients; Thus;  $Z_j$ 's are linear combination with coefficient  $a_{1j}, a_{2j}, \dots, a_{pj}$  and

$$Z_{ij} = (a_{1j}, a_{2j}, \dots, a_{pj}) \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_p \end{bmatrix} \quad (3.2)$$

$$\text{And } Z_1 = a_{i1}X, Z_2 = a_{i2}X, \dots, Z_p = a_{ip}X \quad (3.3)$$

The procedures try to obtain  $a_{ij}$  so that  $Z_j$ , the  $j^{\text{th}}$  PC of X will have the following properties

(i)The Z's are orthogonal

(ii)Each Z capture the maximum variable remaining in X, hence we maximize the variation in Z subject to the constraint  $a_i a_i = 1$

For instance if  $Z_1$  is the first PC we seek for  $a_1$ , such that

$$(i) \text{Var}(Z_1) = \text{Var}(Z_1 X) = a_1 \text{Var}(X) a_1 = a_{11}, \sum a_1 \text{ is a maximum}$$

$$(ii) a_{11} a_1 = \sum a_1^2 = 1$$

If  $Z_2$  is the second PC after determining  $Z_1$ , and it's uncorrelated with  $Z_1$ , we seek for  $a_2$  such that;

$$(i) \text{Var}(Z_2) = a_{22} \text{Var}(X) a_2 = a_{22} \sum a_2 \text{ is a maximum}$$

$$(ii) a_{22} a_2 = \sum a_2^2 = 1$$

$$(iii) a_{11} a_2 = 0, \text{ that is, } Z_1 \text{ and } Z_2 \text{ are orthogonal}$$

The procedure continue in this way to select the  $j^{\text{th}}$  PC such that;

$$(i) \text{Var}(Z_j) = \text{Var}(a_j^1 X) = a_{jj} \sum a_j \text{ is a maximum}$$

$$(ii) a_{jj} a_j = \sum a_j^2 = 1$$

$$(iii) a_{ij} a_m = 0, j \neq m \text{ i.e., } Z_j \text{'s are orthogonal}$$

### The procedure of finding the first pc

To find the first PC, we seek for  $a_1$ , such that

$$Z_1 = a_{11} X_1 + a_{21} X_2 + \dots + a_{p1} X_p = a_1 X \quad (3.4)$$

is the PC of  $X$  subjected to the constant.

$$(i) \text{Var}(Z_1) = \text{Var}(a_1^1 X) = a_1^1 \sum a, \text{ is a maximum}$$

$$(ii) a_1^1 a_1 = 1$$

To maximize var ( $Z_1$ ) subject to  $a_1^1 a_1$ , we define the langrangian function.

$$L(a_1) = a_1^1 \sum a_1 - \lambda (a_{11} a_1 - 1) \quad (3.5)$$

$\lambda$  is the langrangian multiplier.

To maximize  $L(a_1)$  we differentiate  $L(a_1)$  partially with respect to  $a_1$  and equate the result to zero Thus,

$$\frac{\partial L(a_1)}{\partial a_1} = 2a_1 \sum - 2\lambda a_1 = 0 \quad (3.6)$$

$$\text{And } (\sum - \lambda I) a_1 = 0 \quad (3.7)$$

Where:  $\lambda =$  Eigen vector of  $\sum a_1$  is the corresponding Eigen vector of  $\lambda$

The solution  $a_1 = 0$  is a trivial solution and since  $a_1$  cannot be zero (i.e.  $a_1 \neq 0$ ) to have non-trivial solution then  $(\sum - \lambda I) = 0$

(3.8)

and implies that  $\sum = \lambda I$

(3.9)

If (3.7) is to have non-trivial solution, then because of (3.8),  $\lambda$  must be the characteristics root of  $\sum$ .

Hence we will have P characteristic root and P  $a_i$ 's which are vector since  $\sum$  is a P x P dimensional matrix lets  $\lambda_1, \lambda_2, \dots, \lambda_p$  be the characteristic roots of  $\sum$ , then  $\text{var}(Z_1) = a_1' \lambda a_1 = \lambda$

hence  $\max \text{var}(Z_1)$ , is equivalent to  $\max(\lambda)$ . That is, if we have P  $\lambda$ 's we choose the maximum and  $\text{Var}(Z_1) = \lambda_i$ .

### The Procedure for Finding the Second PC

Let  $Z_2$  be the second PC of X, then  $Z_2 = a_{2i} X$ .

We seek  $a_2$  such that;

(i)  $\text{Var}(Z_2) = a_{2i} \sum a_2$  is a maximum

(ii)  $a_{2i} a_2 = 1$

(iii)  $a_{1i} a_2 = 0$

The langrangian function is

$$L(a_2) = a_{2i} \sum a_2 - \lambda(a_{2i} a_2 - 1) - \theta a_{1i} a_2 \quad (3.10)$$

Thus;

$$\begin{aligned} \frac{\partial L(a_2)}{\partial a_2} &= 2a_{2i} \sum - 2\lambda a_2 - \theta_{a1} = 0 \\ &= 2(\sum - \lambda I)a_2 - \theta_{a1} = 0 \end{aligned} \quad (3.11)$$

Multiply by  $a_i$  to get;

$$2a_{1i} \sum a_2 - 2a_{1i} \lambda a_2 - a_{1i} \theta_{a1} = 0$$

$$2a_{1i} \sum a_2 - \theta = 0$$

$$2a_{1i} \lambda a_2 - \theta = 0$$

$$2a_{1i} \lambda a_2 - \theta = 0$$

$$2(\sum -\lambda I)a_2 = 0$$

$$(\sum -\lambda I)a_2 = 0 \quad (3.12)$$

$$\sum a_2 = \lambda a_2$$

### Interpretation of the principal components

The *loading* or the eigenvector  $\alpha_j = \alpha_{j1}, \alpha_{j2}, \dots, \alpha_{jp}$ , is the measure of the importance of a measured variable for a given PC. When all elements are positive, the first component is a weighted average of the variables and is sometimes referred to as measure of *overall crime rate*. Likewise, the positive and negative coefficients in subsequent components may be regarded as *type of crime* components (Rencher, 2002 and Printcom, 2003). The plot of the first two or three loadings against each other enhances visual interpretation (Soren, 2006).

The *score* is a measure of the importance of a PC for an observation. The new PC observations  $Y_{ij}$  are obtained simply by substituting the original variables  $X_{ij}$  into the set of the first PCs. This gives

$$Y_{ij} = \alpha'_{j1}X_{i1} + \alpha'_{j2}X_{i2} + \dots + \alpha'_{jp}X_{ip} \quad (3.13)$$

$$i=1,2,\dots,n, \quad j=1,2,\dots,p$$

### The proportion of Variance

The proportion of variance tells us the PC that best explained the original variables. A measure of how well the first  $q$  PCs of  $Z$  explain the variation is given by:

A cumulative 
$$\psi_q = \frac{\sum_{j=1}^q \lambda_j}{P} = \frac{\sum_{j=1}^q \text{Var}(Z_j)}{P}$$
 is a useful criterion for determining the number of components to be retained in the analysis. A Scree plot provides a good graphical representation of the ability of the PCs to explain the variation in the data (Cattell, 1966).

## ANALYSIS AND RESULTS

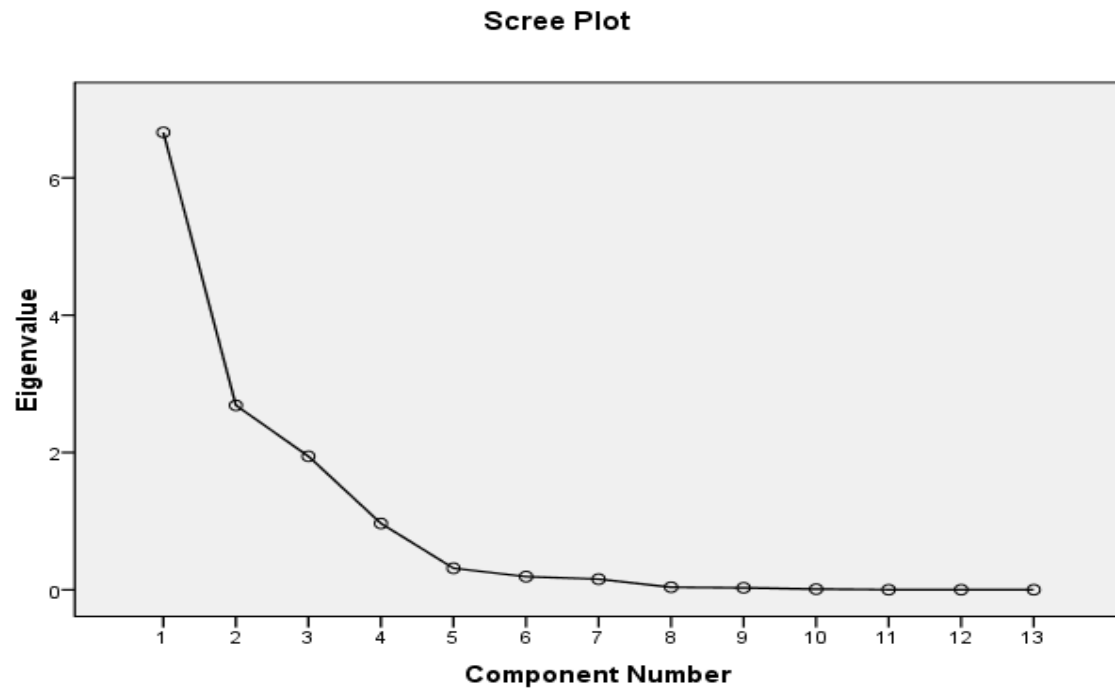
In this section, we present the results of the analysis of the data on the total number of crime committed yearly from 1995 through 2014 in Gwagwalada Area Command, Abuja, Nigeria. The data was collected from the police headquarters, Abuja.

**Table 1: Correlation matrix of Crime Types (per 10,000 Population) in Gwagwalada,****Abuja**

		Rape	Robb ery	GHW	Thef t	V. Theft	Assa ult	Murd er	Burgl ary	C/ Stealin g	Unlaw ful posses sion	Breach of Public Peace	Brok en Store	Unlaw ful Escape
Rape	Pearson Correlation	1	.883**	.930**	.909**	.304	.912**	.857**	-.046	.306	.055	-.007	-.011	.837**
	Sig. (2-tailed)		.000	.000	.000	.193	.000	.000	.846	.189	.818	.978	.962	.000
Robbery	Pearson Correlation	.883**	1	.965**	.925**	.094	.927**	.767**	-.089	.101	.314	.129	.054	.985**
	Sig. (2-tailed)	.000		.000	.000	.693	.000	.000	.708	.671	.177	.588	.822	.000
GHW	Pearson Correlation	.930**	.965**	1	.980**	.227	.980**	.822**	-.028	.231	.321	.206	.116	.922**
	Sig. (2-tailed)	.000	.000		.000	.337	.000	.000	.908	.327	.167	.384	.627	.000
Theft	Pearson Correlation	.909**	.925**	.980**	1	.312	.998**	.803**	-.016	.310	.322	.222	.138	.883**
	Sig. (2-tailed)	.000	.000	.000		.181	.000	.000	.945	.184	.166	.346	.561	.000
V. Theft	Pearson Correlation	.304	.094	.227	.312	1	.298	.249	.083	.998**	-.013	.070	.280	.115
	Sig. (2-tailed)	.193	.693	.337	.181		.202	.290	.729	.000	.957	.769	.232	.628
Assault	Pearson Correlation	.912**	.927**	.980**	.998**	.298	1	.808**	-.021	.296	.314	.210	.111	.882**
	Sig. (2-tailed)	.000	.000	.000	.000	.202		.000	.928	.205	.177	.374	.642	.000
Murder	Pearson Correlation	.857**	.767**	.822**	.803**	.249	.808**	1	.052	.237	.096	.076	-.078	.738**
	Sig. (2-tailed)	.000	.000	.000	.000	.290	.000		.829	.315	.687	.751	.745	.000
Burglary	Pearson Correlation	-.046	-.089	-.028	-.016	.083	-.021	.052	1	.071	.226	.222	.119	-.094
	Sig. (2-tailed)	.846	.708	.908	.945	.729	.928	.829		.767	.338	.346	.616	.692
C/Stealin g	Pearson Correlation	.306	.101	.231	.310	.998**	.296	.237	.071	1	-.006	.080	.297	.119
	Sig. (2-tailed)	.189	.671	.327	.184	.000	.205	.315	.767		.982	.736	.204	.617
Unlawfu l possessi on	Pearson Correlation	.055	.314	.321	.322	-.013	.314	.096	.226	-.006	1	.892**	.744**	.310
	Sig. (2-tailed)	.818	.177	.167	.166	.957	.177	.687	.338	.982		.000	.000	.183
Breach of Public Peace	Pearson Correlation	-.007	.129	.206	.222	.070	.210	.076	.222	.080	.892**	1	.849**	.090
	Sig. (2-tailed)	.978	.588	.384	.346	.769	.374	.751	.346	.736	.000		.000	.707
Broken Store	Pearson Correlation	-.011	.054	.116	.138	.280	.111	-.078	.119	.297	.744**	.849**	1	.054
	Sig. (2-tailed)	.962	.822	.627	.561	.232	.642	.745	.616	.204	.000	.000		.821
Unlawfu l Escape	Pearson Correlation	.837**	.985**	.922**	.883**	.115	.882**	.738**	-.094	.119	.310	.090	.054	1
	Sig. (2-tailed)	.000	.000	.000	.000	.628	.000	.000	.692	.617	.183	.707	.821	

\*\*. Correlation is significant at the 0.01 level (2-tailed).

**Source:** Derived from Statistics Department of the Nigeria Police Force, Abuja



**Fig. 1:** Scree Plot

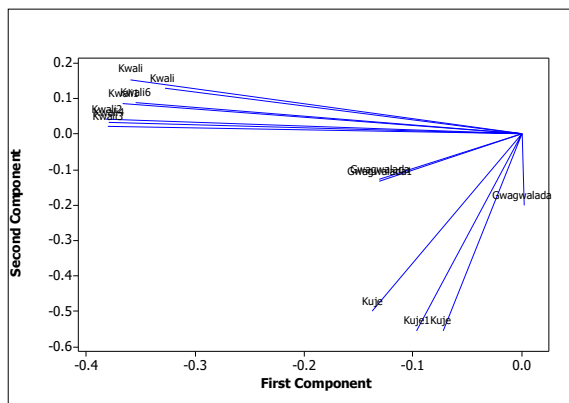
**Table 2: Eigenvalues**

Component	Initial Eigenvalues		
	Eigenvalues	Proportion	Cumulative
1	6.663	51.251	51.251
2	2.686	20.664	71.916
3	1.944	14.957	86.873
4	.966	7.433	94.306
5	.314	2.415	96.720
6	.192	1.478	98.198
7	.155	1.196	99.394
8	.037	.288	99.681
9	.029	.222	99.904
10	.010	.073	99.977
11	.002	.013	99.990
12	.001	.008	99.998
13	.000	.002	100.000

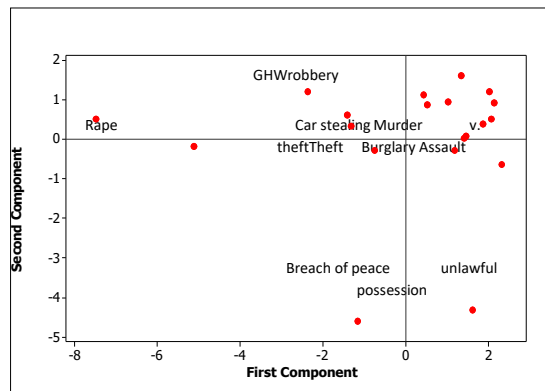


**Table 3: Eigenvectors**

Variable	PC1	PC2	PC3	PC4	PC5	PC6	PC7	PC8	PC9	PC10	PC11	PC12	PC13
Rape	-0.359	0.154	-0.050	-0.039	-0.158	0.468	-0.060	0.686	0.061	0.318	0.106	0.074	0.066
Robbery	-0.367	0.086	0.160	0.045	-0.269	0.021	0.194	-0.028	0.342	-0.027	-0.623	0.149	-0.438
GHW	-0.382	0.042	0.070	-0.002	-0.041	0.058	-0.178	0.056	0.229	-0.789	0.341	-0.130	-0.002
Theft	-0.380	0.021	0.010	0.002	-0.043	-0.034	-0.424	-0.294	-0.293	0.052	-0.030	0.669	0.220
V. theft	-0.131	-0.127	-0.655	0.042	-0.071	-0.166	0.046	-0.005	-0.042	0.098	0.353	0.136	-0.589
Assault	-0.380	0.032	0.017	-0.003	-0.030	-0.082	-0.445	-0.177	-0.246	0.261	-0.117	-0.680	-0.115
Murder	-0.328	0.129	-0.017	-0.185	0.726	-0.203	0.439	-0.121	-0.214	-0.097	-0.097	-0.016	-0.007
Burglary	0.002	-0.202	-0.042	-0.951	-0.177	0.134	0.006	-0.061	0.020	0.002	-0.012	-0.008	-0.003
Car stealing	-0.131	-0.133	-0.652	0.061	-0.095	-0.122	0.052	0.072	0.185	-0.099	-0.369	-0.120	0.557
Unlawful Possession	-0.137	-0.501	0.256	0.023	-0.188	-0.483	0.100	0.507	-0.346	-0.072	-0.038	0.030	0.015
Breach of peace	-0.097	-0.555	0.157	0.046	0.362	-0.115	-0.188	-0.135	0.610	0.261	0.124	0.041	0.030
Broken store	-0.072	-0.554	-0.030	0.218	0.014	0.647	0.214	-0.216	-0.313	-0.131	-0.084	-0.065	-0.045
Unlawful escape	-0.356	0.087	0.143	0.058	-0.399	-0.051	0.510	-0.249	0.091	0.294	0.420	-0.080	0.286



(a)



(b)

**Fig. 2: Loading and score plot for the first and second Principal Component (PC)**

**DISCUSSION OF RESULTS**

The correlation matrix in Table 1 displayed different levels of correlation between the crimes. There is strong positive relationship in between robbery, rape, grievous hurt and wound (GHW), theft, assault, murder, and unlawful escape, unlawful possession and breach of public peace, c/stealing and v.theft. Their relationship were also significant at 5% significance level., which means that their variables can be used to predict (explain) one another. Similarly, it was observed that the correlations between robbery and burglary, breach of public peace and broken store, rape and burglary, GHW and burglary, theft and burglary, assault and burglary, murder and broken store, c/stealing and unlawful possession were negative and insignificant.

The eigenvalues, proportion and the cumulative proportions of the explained variance are displayed in Table 2. Considering the eigenvalue-one criterion and the Scree plot in figure 1, it would be reasonable to retain the first four PCs. A commonly accepted rule says that it suffices to keep only PCs with eigenvalues larger than 1. However, the fourth eigenvalues  $\lambda=0.966$  and are approximately close to 1, so that the first 4 PCs can be retain to explain up to 94.306 percent of the total variability.

From Table 3, the first PC combines the number of all the crimes with approximately positive constant (0.002 – 0.669) weight, and is interpreted as the overall measure of crime. From figure 2a, Gwagwalada Area Council has the overall crime rate, while Kwali have the lowest crime rate.

The second PC on figure 2(b) has classified the crimes into groups: (1) the concentrated crimes consisting of rape, GHW, car stealing, robbery, murder, rape and vehicle theft (2) Assault, burglary, breach of peace and unlawful possession.

From Figure 2(b), rape is an outlier and is located at the upper side, and G.H.W. is located at the right part. Therefore, from Figure 2(a), the Area Council at the upper side show tendency towards rape, therefore Kwali Area Council has the highest prevalence for rape. Gwagwalada Area Council shows tendency towards G.H.W., robbery, Assault, murder, car stealing, Vehicle theft and theft while breach of peace and unlawful possession are located at the lower part of figure 2a, i.e. Kuje Area Council.

## CONCLUSION

The following are the conclusions deduced from the analysis. There is strong positive relationship between robbery and rape, grievous hurt and wound (GHW), theft, assault, murder and unlawful escape, the relationship were also significant, which means that their variables can be used to predict (explain) one another. It was also observed that the correlations in between robbery and burglary, breach of public peace and broken store were negative and insignificant. The Area Council with the highest crime rate is Gwagwalada, Kuje has a moderate crime rate, while Kwali Area Council have the lowest crime rate in Abuja. Four PCs that explains about 94.306per cent of the total variability of the data set are suggested to be retained.

The second component has classified the crimes into two, namely, (1) concentrated offences: Rape, G.H.W., vehicle theft, theft, Car stealing, robbery, Murder (2) less concentrated: murder and robbery. Base on this, the component has geographically divided Gwagwalada Area Command between the north and south in relation to the crime classifications. The southern parts of A Contain more assault, breach of peace, theft, vehicle theft, while the northern part has the prevalence of the concentrated crimes like rape, GHW, robbery, murder, car stealing. This will help inidentifying the distribution of crimes in Gwagwalada, Abuja, allowing the investors to measure the level of risk and to plan how preventive measures for safeguarding their investments.

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